

1. Ecuaciones generales

1.	Ec. cinemáticas	$\nabla \mathbf{u} = \mathbf{S} + \boldsymbol{\Omega} \quad (S_{ij} = S_{ji}) \quad (\Omega_{ij} = -\Omega_{ji})$ $\nabla \cdot \mathbf{u} = S_{11} + S_{22} + S_{33} \quad (\text{expansión})$ $\nabla \times \mathbf{u} = -\Omega_{23} \hat{\mathbf{e}}_1 + \Omega_{13} \hat{\mathbf{e}}_2 - \Omega_{12} \hat{\mathbf{e}}_3 \quad (\text{vorticidad})$
2.	Ec. de continuidad	$\frac{d\rho}{dt} + \rho \nabla \cdot \mathbf{u} = 0 \quad \text{o bien} \quad \frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{u}) = 0$
3.	Ec. de movimiento (forma integral)	$\rho \frac{d\mathbf{u}}{dt} = \mathbf{f}_V + \nabla \cdot \mathbf{T} \quad \text{o bien} \quad \rho \frac{\partial \mathbf{u}}{\partial t} + \rho (\mathbf{u} \cdot \nabla) \mathbf{u} = \mathbf{f}_V + \nabla \cdot \mathbf{T}$ $\int_V \rho \frac{d\mathbf{u}}{dt} dV = \int_V \mathbf{f}_V dV + \int_{S(V)} \mathbf{T} \cdot \hat{\mathbf{n}} dS \quad \text{o bien}$ $\int_V \rho \frac{\partial \mathbf{u}}{\partial t} dV + \int_{S(V)} \rho \mathbf{u} (\mathbf{u} \cdot \hat{\mathbf{n}}) dS = \int_V \mathbf{f}_V dV + \int_{S(V)} \mathbf{T} \cdot \hat{\mathbf{n}} dS$
4.	Ec. de la energía	$\rho \frac{de}{dt} = T_{ij} S_{ij} - \nabla \cdot \mathbf{q} + Q_v$

2. Casos particulares ($q = 0$, $Q_V = 0$)

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| 1. Campo gravitatorio | $\mathbf{f}_V = \rho \mathbf{g}$ | $\Rightarrow \mathbf{f}_V = -\rho \nabla \varphi$ |
| 2. Flujo nulo (hidrostático) | $\mathbf{u} = 0$ | $\Rightarrow \mathbf{T} = -p \mathbb{I} \quad , \quad \nabla \cdot \mathbf{T} = -\nabla p = -\mathbf{f}_V$ |
| 3. Flujo incompresible | $\nabla \cdot \mathbf{u} = 0$ | $\Rightarrow \mathbf{u} = \nabla \times \mathbf{A} \quad , \quad \nabla(\nabla \cdot \mathbf{A}) - \nabla^2 \mathbf{A} = \boldsymbol{\omega}$ |
| 4. Flujo incompresible-plano | $\mathbf{A} = \psi \hat{\mathbf{z}}$ | $\Rightarrow \nabla^2 \psi = -\omega$ |
| 5. Flujo irrotacional | $\nabla \times \mathbf{u} = 0$ | $\Rightarrow \mathbf{u} = \nabla \phi \quad , \quad \nabla^2 \phi = S_{11} + S_{22} + S_{33}$ |
| 6. Flujo irrotacional-plano | $\phi(x_1, x_2)$ | $\Rightarrow \nabla^2 \phi = S_{11} + S_{22}$ |
| 7. Flujo irrot-incomp-plano | (4-6) | $\Rightarrow \nabla^2 \phi = 0 \quad , \quad \nabla^2 \psi = 0$ |
| 8. Fluido ideal | $\mathbf{T} = -p \mathbb{I}$ | $\Rightarrow \nabla \cdot \mathbf{T} = -\nabla p$ |
| si es barotrópico | $\rho = f(p)$ | $\Rightarrow \nabla p = \rho \nabla \mathcal{P}$ |
| además uniforme | $\rho = \rho_0$ | $\Rightarrow \nabla(p/\rho_0) = \nabla \mathcal{P}$ |
| no-estacionario | $\mathbf{u}(\mathbf{x}, t)$ | $\Rightarrow \partial_t \mathbf{u} + \nabla(\mathcal{P} + u^2/2) + \boldsymbol{\omega} \times \mathbf{u} = \mathbf{f}_V/\rho_0$ |
| e irrotacional | | $\Rightarrow \nabla(\partial_t \phi + \mathcal{P} + u^2/2) = \mathbf{f}_V/\rho_0$ |
| y gravitatorio | | $\Rightarrow \nabla(\partial_t \phi + \mathcal{P} + \varphi + u^2/2) = 0$ |
| estacionario | $\mathbf{u} = \mathbf{u}(\mathbf{x})$ | $\Rightarrow \nabla(\mathcal{P} + u^2/2) + \boldsymbol{\omega} \times \mathbf{u} = \mathbf{f}_V/\rho_0$ |
| incompresible | $\nabla \cdot \mathbf{u} = 0$ | $\Rightarrow \mathbf{u} \cdot \nabla(\mathcal{P} + u^2/2) = \mathbf{u} \cdot \mathbf{f}_V/\rho_0$ |
| y gravitatorio | | $\Rightarrow \mathbf{u} \cdot \nabla(\mathcal{P} + \varphi + u^2/2) = 0$ |