

07/10

Práctica 2

Int. LU₆-Matriz

1) $\mathbb{R}^m \times \mathbb{R}^n$ de LU_6
 \times de líneas esp.

2) Reglas de selección



3) Distancia hamiltoniana

Doppler

En Sencheminto Doppler

$$\Delta \omega_D = 2\sqrt{z} \omega \cdot \frac{v_w}{c} \quad v_w^2 = \frac{2k_B T}{m}$$

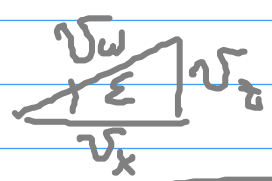
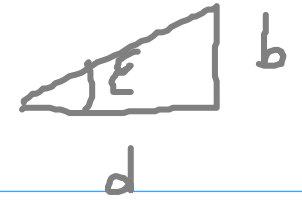
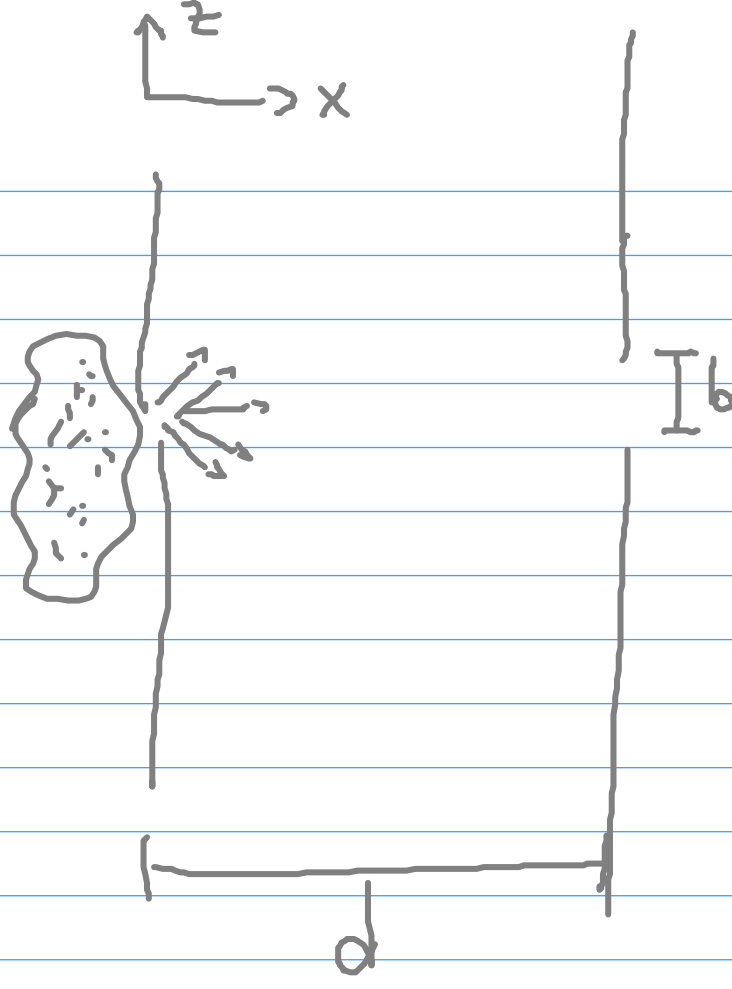
$$\left[\omega = 2\pi \cdot \nu = 2\pi f \quad T = \frac{1}{\nu} = \frac{2\pi}{\omega} \right]$$

$$\Delta \nu_D = 7,16 \cdot 10^{-7} \times \nu_0 \sqrt{\frac{T}{M}} \text{ Hz}$$

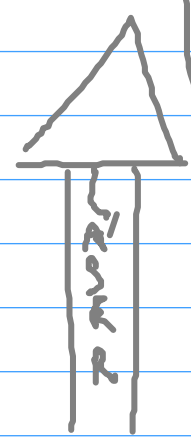
$$[\nu_0] = \text{Hz}$$

$$[M] = \frac{[T] = \text{K}}$$

$M \rightarrow$ molar mass
(g/mol)



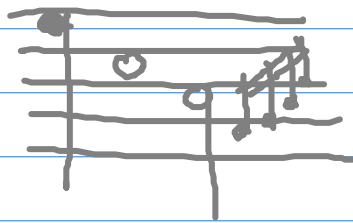
$$|v_z| < v \sin \epsilon$$



$v \sin \epsilon$

$$\Delta \ll \Delta t \approx \frac{1}{2\pi}$$

↳ Como llega de acá
a $\Delta p \Delta x > \hbar c$?



Quantum theory
Asher
Peres

Coeffs. de Einstein

$$\boxed{\text{diagrama}} \quad \text{--- } \hbar \omega \quad \Delta(\omega) \rightarrow \Gamma$$

$$\left. \frac{dP^{A \leftrightarrow B}}{dt} \right|_{EM} = B \int \rho(\omega) \Delta(\omega) d\omega$$

$$\left. \frac{dP}{dt} \right|_{S} \approx B \int \rho(\omega) \Delta(\omega) d\omega$$

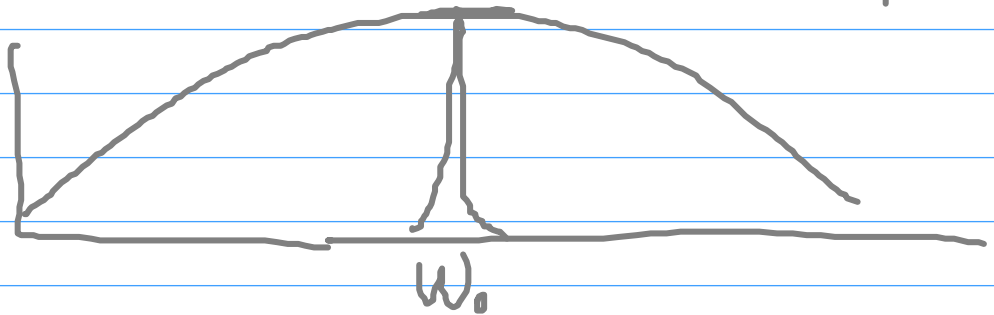
$$\left. \frac{dP^S}{dt} \right| = A \quad \boxed{B = \frac{\lambda^3}{8\pi\hbar} A}$$

$$A = \Gamma$$

-) Espectro es ancho
-) Monocromática

Broad band

$$\int \mathcal{P}(\omega) \Delta(\omega) d\omega = \mathcal{P}(\omega_0) \underbrace{\int \Delta(\omega) d\omega}_1$$



$$\Delta(\omega) = \frac{\Gamma/\sqrt{2\pi}}{(\omega - \omega_0)^2 + (\Gamma/2)^2}$$

N atomos N_1, N_2

$$\left\{ \frac{dN_2}{dt} = -\Gamma N_2 + B \mathcal{P}(\omega_0) (N_1 - N_2) \right.$$

$$0 = -\Gamma N_2 + B \mathcal{P} (N_1 - N_2)$$

$$\Rightarrow (\Gamma + B \mathcal{P}) N_2 = B \mathcal{P} N_1$$

$$N_2 = \frac{B \mathcal{P}}{\Gamma + B \mathcal{P}} N_1$$

$$N_2 = \frac{B\rho}{\Gamma + B\rho} N_1 \quad S = \frac{2B\rho}{\Gamma}$$

$$N_2 = \frac{1}{1 + \Gamma/B\rho} N_1 = \frac{1}{1 + 2/S} N_1$$

$$N = N_1 + N_2 \Rightarrow N_1 = N - N_2$$

$$\Rightarrow N_2 = \frac{S}{S+1} \frac{N}{2} \quad \text{si } S \rightarrow \infty \quad N_2 = \frac{N}{2}$$

$$\frac{dW}{dt} = \hbar\omega \left(\frac{dP^{\text{abs}}}{dt} - \frac{dP^{\text{Em}}}{dt} \right) =$$

$$= \hbar\omega (B\rho N_1 - B\rho N_2)$$

$$= \hbar\omega \frac{\Gamma}{2} \frac{S}{S+1} N$$

$$\xrightarrow{S \rightarrow \infty} \frac{dW}{dt} = \hbar\omega \frac{\Gamma}{2} N$$

$$\text{Para 1 átomo: } \frac{dW}{dt} = \hbar\omega \frac{\Gamma}{2}$$

Monocromático

$$\int \rho(\omega) \Delta(\omega) d\omega$$

$$\rho(\omega) = \delta(\omega - \omega_L) \frac{I}{c}$$

$$\rightarrow \Delta(\omega_L) \frac{I}{c}$$

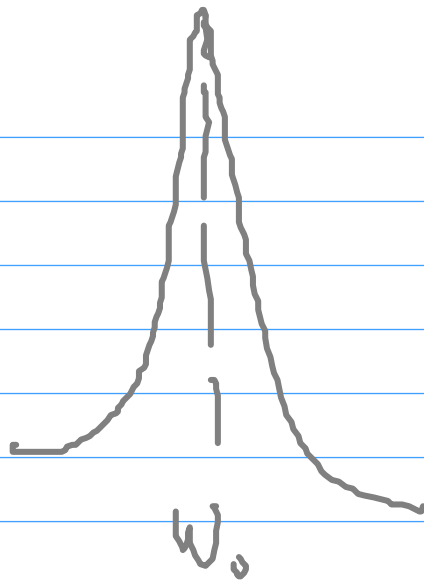
$$\frac{dN_2}{dt} = -A N_2 + B \frac{I}{c} \Delta(\omega) (N_1 - N_2)$$

$$\sigma(\omega) = A \frac{\lambda_0^2}{4} \Delta(\omega) \quad B = \frac{\lambda_0^3}{8\pi^2 \hbar} A$$

$$\Rightarrow \frac{dN_2}{dt} = -\Gamma N_2 + \frac{\sigma(\omega_L) I}{\hbar \omega_0} (N_1 - N_2)$$

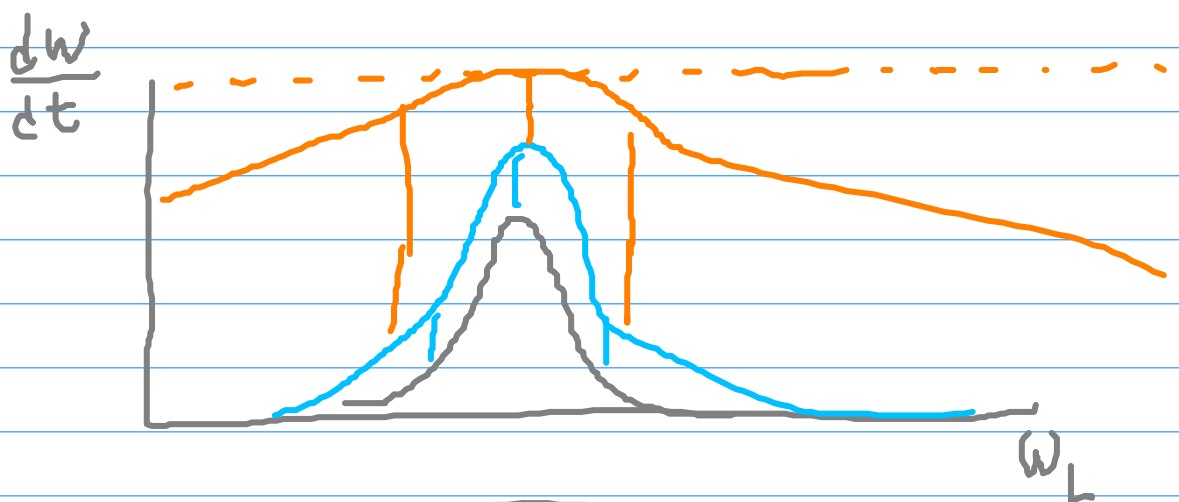
$$S(\omega_L) = \frac{2\sigma(\omega_L) I}{\hbar \omega_0 \Gamma}$$

N_1	N_2	N
n ^o de át en F_1	n ^o de át en elec	n ^o de átomos
$ \langle \psi \alpha_1 \rangle ^2$	$ \langle \psi \alpha_2 \rangle ^2$	1
P_{11}	P_{22}	



Si resolvemos para el
estacionario:

$$\frac{dW}{dt} = h w_0 \frac{\Gamma}{2} \frac{S(w_L)}{S(w_L)+1} N$$



Bibliografía: Demtröder
Cap 7

Budker, de eó.
Cap 3