

$$dW_g = \vec{F}_g \cdot d\vec{\ell}$$

$$d\vec{\ell} = dx \hat{x}$$
$$\vec{F}_g = mg(-\cos\theta \hat{y} + \sin\theta \hat{x})$$

$$dW_g = mg \sin\theta dx$$

$$\frac{dW_g}{dt} = mg \sin\theta \frac{dx}{dt} = mg \sin\theta v$$

$$\frac{dW_g}{dt} = mg \sin\theta \cdot \frac{mg R \sin\theta}{(Be)^2 \omega^2 \theta}$$

$$\frac{dW_g}{dt} = \frac{(mg)^2}{(Be)^2} \cdot R \frac{\sin^2\theta}{\cos^2\theta} = P_{\text{Joule}}$$

$$\frac{dW_g}{dt} = P_{\text{Joule}} = \left( \frac{mg \tan\theta}{Be} \right)^2 R$$