

Electrodinámica:

($\hat{\mathbf{n}}$ tiene dirección $1 \rightarrow 2$. En los conductores, se asume que el conductor es el medio 1)

Material	Coefficientes del medio	Condición de Contorno
<p>Dieléctricos sin pérdidas</p> <p>ϵ, μ reales</p>	$\epsilon = D/E$ $n = ck/\omega = \sqrt{\mu\epsilon}$ $\eta = E/H = \sqrt{\mu/\epsilon}$	$(\mathbf{E}_2 - \mathbf{E}_1) \times \hat{\mathbf{n}} = 0 \text{ (útil; ver abajo)}$ $(\mathbf{D}_2 - \mathbf{D}_1) \cdot \hat{\mathbf{n}} = 0$ $(\mathbf{B}_1 - \mathbf{B}_2) \cdot \hat{\mathbf{n}} = 0$ $(\mathbf{H}_1 - \mathbf{H}_2) \times \hat{\mathbf{n}} = 0 \text{ (útil; ver abajo)}$
<p>Dieléctricos con pérdidas</p> <p>μ real</p>	$\epsilon = D/E = \epsilon_r + i\epsilon_i$ $n = ck/\omega = \sqrt{\mu\epsilon_r} (1 + i\epsilon_i/\epsilon_r)^{1/2}$ $\eta = E/H = \sqrt{\mu/\epsilon_r} (1 + i\epsilon_i/\epsilon_r)^{-1/2}$	$(\mathbf{E}_2 - \mathbf{E}_1) \times \hat{\mathbf{n}} = 0 \text{ (útil; ver abajo)}$ $(\mathbf{D}_2 - \mathbf{D}_1) \cdot \hat{\mathbf{n}} = 0$ $(\mathbf{B}_1 - \mathbf{B}_2) \cdot \hat{\mathbf{n}} = 0$ $(\mathbf{H}_1 - \mathbf{H}_2) \times \hat{\mathbf{n}} = 0 \text{ (útil; ver abajo)}$
<p>Conductores perfectos</p>	$\mathbf{E}_c = 0$	$\mathbf{E}_2 \times \hat{\mathbf{n}} = 0 \text{ (útil; ver abajo)}$ $\mathbf{H}_2 \times \hat{\mathbf{n}} = -(4\pi/c) \mathbf{g}_L$
<p>Conductores reales</p> <p>ϵ, μ real</p>	$\sigma = J/E$ $n = ck/\omega = \sqrt{\mu\epsilon} [1 + i4\pi\sigma/(\omega\epsilon)]^{1/2}$ $\eta = E/H = \sqrt{\mu/\epsilon} [1 + i4\pi\sigma/(\omega\epsilon)]^{-1/2}$	$(\mathbf{E}_2 - \mathbf{E}_1) \times \hat{\mathbf{n}} = 0 \text{ (útil; ver abajo)}$ $(\mathbf{D}_2 - \mathbf{D}_1) \cdot \hat{\mathbf{n}} = 0$ $(\mathbf{B}_1 - \mathbf{B}_2) \cdot \hat{\mathbf{n}} = 0$ $(\mathbf{H}_c - \mathbf{H}_2) \times \hat{\mathbf{n}} = 0 \text{ (útil; ver abajo)}$
<p>Plasma diluido</p> <p>ϵ, μ real</p>	$\sigma(\omega) = J/E = i\omega_p^2/(4\pi\omega)$ $n = ck/\omega = \sqrt{\mu\epsilon} [1 - \omega_p^2/(\epsilon\omega^2)]^{1/2}$ $\eta = E/H = \sqrt{\mu/\epsilon} [1 - \omega_p^2/(\epsilon\omega^2)]^{-1/2}$	$(\mathbf{E}_2 - \mathbf{E}_1) \times \hat{\mathbf{n}} = 0 \text{ (útil; ver abajo)}$ $(\mathbf{D}_2 - \mathbf{D}_1) \cdot \hat{\mathbf{n}} = 0$ $(\mathbf{B}_1 - \mathbf{B}_2) \cdot \hat{\mathbf{n}} = 0$ $(\mathbf{H}_c - \mathbf{H}_2) \times \hat{\mathbf{n}} = 0 \text{ (útil; ver abajo)}$

Incidencia sobre una capa material:

1 = medio incidente, 2 = capa material y 3 = medio transmitido. Contorno 1-2 en $z = 0$ y contorno 2-3 en $z = -d$

textbfnota: en el caso de un conductor perfecto: $E_c = 0$ y $H_c = 0$. No usar las siguientes relaciones!

Modo	Condiciones de contorno	Ángulos e impedancias
T.E. ($z = 0$)	$E_i^{(1)} + E_r^{(1)} = E_i^{(2)} + E_r^{(2)}$ $E_i^{(1)} \cos \theta_1 / \eta_1 - E_r^{(1)} \cos \theta_1 / \eta_1 = E_i^{(2)} \cos \theta_2 / \eta_2 - E_r^{(2)} \cos \theta_2 / \eta_2$	$n_1 \sin \theta_1 = n_2 \sin \theta_2$
T.E. ($z = -d$)	$E_t^{(2)} e^{ik_2 d \cos \theta_2} + E_r^{(2)} e^{-ik_2 d \cos \theta_2} = E_t^{(2)} e^{ik_3 d \cos \theta_3}$ $E_t^{(2)} e^{ik_2 d \cos \theta_2} \cos \theta_2 / \eta_2 - E_r^{(2)} e^{-ik_2 d \cos \theta_2} \cos \theta_2 / \eta_2 = E_t^{(3)} e^{ik_3 d \cos \theta_3} \cos \theta_3 / \eta_3$	$n_2 \sin \theta_2 = n_3 \sin \theta_3$
T.M. ($z = 0$)	$E_i^{(1)} \cos \theta_1 - E_r^{(1)} \cos \theta_1 = E_i^{(2)} \cos \theta_2 - E_r^{(2)} \cos \theta_2$ $E_i^{(1)} / \eta_1 + E_r^{(1)} / \eta_1 = E_i^{(2)} / \eta_2 + E_r^{(2)} / \eta_2$	$n_1 \sin \theta_1 = n_2 \sin \theta_2$
T.M. ($z = -d$)	$E_t^{(2)} e^{ik_2 d \cos \theta_2} \cos \theta_2 - E_r^{(2)} e^{-ik_2 d \cos \theta_2} \cos \theta_2 = E_t^{(2)} e^{ik_3 d \cos \theta_3} \cos \theta_3$ $E_t^{(2)} e^{ik_2 d \cos \theta_2} / \eta_2 + E_r^{(2)} e^{-ik_2 d \cos \theta_2} / \eta_2 = E_t^{(3)} e^{ik_3 d \cos \theta_3} / \eta_3$	$n_2 \sin \theta_2 = n_3 \sin \theta_3$

$$\begin{cases} \tilde{n}_1 = n_1 \cos \theta_1 & \tilde{n}_2 = n_2 \cos \theta_2 & \tilde{n}_3 = n_3 \cos \theta_3 \\ \tilde{\eta}_1 = \eta_1 / \cos \theta_1 & \tilde{\eta}_2 = \eta_2 / \cos \theta_2 & \tilde{\eta}_3 = \eta_3 / \cos \theta_3 \\ \tilde{k}_1 = \tilde{n}_1 \omega / c & \tilde{k}_2 = \tilde{n}_2 \omega / c & \tilde{k}_3 = \tilde{n}_3 \omega / c \end{cases} \quad (1)$$

Modo T.E.:

$$\rho = \frac{E_r^{(1)}}{E_i^{(1)}} = \frac{\left(1 - \frac{\tilde{\eta}_1}{\tilde{\eta}_3}\right) \cos(\tilde{k}_2 d) + i \left(\frac{\tilde{\eta}_1}{\tilde{\eta}_2} - \frac{\tilde{\eta}_2}{\tilde{\eta}_3}\right) \text{sen}(\tilde{k}_2 d)}{\left(1 + \frac{\tilde{\eta}_1}{\tilde{\eta}_3}\right) \cos(\tilde{k}_2 d) - i \left(\frac{\tilde{\eta}_1}{\tilde{\eta}_2} + \frac{\tilde{\eta}_2}{\tilde{\eta}_3}\right) \text{sen}(\tilde{k}_2 d)} \quad (2)$$

$$\tau' = \frac{E_t^{(3)}(z=0)}{E_i^{(1)}(z=0)} = \frac{2 e^{-i\tilde{k}_3 d}}{\left(1 + \frac{\tilde{\eta}_1}{\tilde{\eta}_3}\right) \cos(\tilde{k}_2 d) - i \left(\frac{\tilde{\eta}_1}{\tilde{\eta}_2} + \frac{\tilde{\eta}_2}{\tilde{\eta}_3}\right) \text{sen}(\tilde{k}_2 d)} \quad (3)$$

$$\tau = \frac{E_t^{(3)}(z=-d)}{E_i^{(1)}(z=0)} = \frac{2}{\left(1 + \frac{\tilde{\eta}_1}{\tilde{\eta}_3}\right) \cos(\tilde{k}_2 d) - i \left(\frac{\tilde{\eta}_1}{\tilde{\eta}_2} + \frac{\tilde{\eta}_2}{\tilde{\eta}_3}\right) \text{sen}(\tilde{k}_2 d)} \quad (4)$$